



**Figure 1**

Pharmacokinetic and pharmacodynamic model of the interaction between SJW and CsA.  $X$  is the daily intake of SJW ( $\text{mg day}^{-1}$ ),  $K_s$  is the rate constant of synthesis of detoxicating proteins ( $\text{AU/month}$ ),  $k_e$  is the elimination rate constant of the detoxicating proteins ( $1/\text{month}$ ),  $P$  is the amount of the detoxicating proteins ( $\text{AU}$ ),  $D$  is the daily dose of CsA ( $\text{mg day}^{-1}$ ),  $C$  is CsA trough blood concentration ( $\text{ng ml}^{-1}$ ),  $K_{s0}$  is the rate constant of detoxicating proteins in the absence of SJW ( $\text{AU/month}$ ),  $I_{\max}$  is the maximal induction potency of SJW for detoxicating proteins,  $K_m$  is the dose of SJW required to induce half-maximal induction ( $\text{mg day}^{-1}$ ), and  $\alpha$  is a constant ( $(\text{ng ml}^{-1})/(\text{mg day}^{-1})/\text{AU}$ )

The intake of SJW is considered to increase  $K_s$ . The analysis in the previous section demonstrated that the extent of decrease in the  $C/D$  ratio of CsA is saturable and SJW dose-dependent. Therefore,  $K_s$  can be described by equation 2:

$$K_s = K_{s0} \cdot \left( 1 + I_{\max} \cdot \frac{X}{X + K_m} \right) \quad (2)$$

where  $K_{s0}$ ,  $X$ ,  $I_{\max}$  and  $K_m$  represent a zero-order synthesis rate constant of  $P$  in the absence of SJW ( $\text{AU/month}$ ), the daily dose of SJW ( $\text{mg day}^{-1}$ ), the maximal induction potency of SJW for  $P$  and the dose of SJW required to induce half-maximal induction ( $\text{mg day}^{-1}$ ), respectively. In each case, the  $C/D$  ratio was assumed to be in inverse proportion to  $P$  for each patient. The relationship between  $C$  and  $D$  can be represented by equation 3:

$$C = \frac{D}{\alpha \cdot P} \quad (3)$$

where  $C$ ,  $D$  and  $\alpha$  represent the trough blood concentration of CsA ( $\text{ng ml}^{-1}$ ), the daily dose of CsA ( $\text{mg day}^{-1}$ ) and a constant ( $(\text{mg day}^{-1})/(\text{ng ml}^{-1})/\text{AU}$ ), respectively. Equation 3 can be rewritten as follows:

$$P = \frac{1}{\alpha} \cdot \frac{D}{C} \quad (3')$$

Substituting equation 3' into equation 1 gives equation 4:

$$\frac{d\frac{D}{C}}{dt} = \alpha \cdot K_s - k_e \cdot \frac{D}{C} \quad (4)$$

Substituting equation 2 into equation 4 gives equation 4':

$$\frac{d\left(\frac{C}{D}\right)^{-1}}{dt} = \alpha \cdot K_{s0} \cdot \left( 1 + \frac{I_{\max} \cdot X}{X + K_m} \right) - k_e \cdot \left(\frac{C}{D}\right)^{-1} \quad (4')$$

#### Model analysis

Equation 4' was simultaneously fitted to the time profiles of  $C/D$  ratio for all the cases, taking the dose profiles of SJW as input functions, by using a nonlinear least-squares method (MLAB, Civilized Software Inc., MD, USA) to obtain common pharmacokinetic parameters,  $I_{\max}$ ,  $K_m$  and  $k_e$ , and an individual parameter for each case,  $\alpha \cdot K_{s0}$ . The  $K_m$  value was modelled based on a log-normal distribution.

#### Results

##### Analysis of the dose–response relationship of SJW for the induction of the detoxicating proteins

The increase in the steady-state  $D/C$  ratio of CsA by SJW was dose-dependent and described by saturable Michaelis-Menten kinetics, suggesting that the induction of detoxicating proteins by SJW is saturable (Figure 2).

##### Model analysis

As a result of model analysis,  $I_{\max}$ ,  $K_m$  and  $k_e$  were calculated to be 2.61, 428 ( $\text{mg day}^{-1}$ ) and 4.72 ( $1/\text{month}$ ), respectively. Moreover the individual parameter values  $\alpha \cdot K_{s0}$ , ranged from 3.33 to 10.0 ( $(\text{mg day}^{-1})/(\text{ng ml}^{-1})/\text{month}$ ) (Table 2). The developed model could adequately explain the observed time profile of the  $C/D$  ratio in each case (Figure 3).

#### Discussion

We have reported a pharmacokinetic model to explain the mechanism-based inhibition of CYP3A4 by grapefruit juice in which the turnover of CYP3A4 protein was incorporated. The model provided the dosing-interval dependency of the extent of interaction based on the time-dependent changes of the active CYP3A4 content [14]. With regard to the induction of detoxicating protein(s), model analysis based on the turnover of protein(s) has not been carried out. CsA concentration is decreased as a result of the induction of detoxicating proteins by SJW intake. Therefore, we employed the  $C/$